# MTH 229 Sec 105 Fall 2015

Course Title/Number	MTH 229: Calculus with Analytic Geometry I (CT); CRN 3077
Semester/Year	Fall 2015
Days/Time	MW 5-5:50pm; TR 5-6:15pm
Location	SH 509
Instructor	Dr. Michael Otunuga
Office	WAEC 3229 (Engineering building)
Office Hours	MTWR 2-3pm, 4-5pm. Others by appointment.
	To make an appointment, email in advance when possible.
Phone	(304) 696-3049
E-Mail	otunuga@marshall.edu
Free tutoring	Free Tutoring in Smith Music Hall 115 and Smith Hall 620 Monday to Friday
Course Description	A careful review of the main techniques of Limits, derivatives and integrals of elementary functions of one variable, including transcendental functions. Applications of derivatives and integrals. Using graphing calculators and Mathematica to solve problems. This course meets a Core I: CT requirement and a Core II: Math requirement
University Policies	By enrolling in this course, you agree to the University Policies listed below. Please read the full text of each policy be going to <a href="www.marshall.edu/academic-affairs">www.marshall.edu/academic-affairs</a> and clicking on "Marshall University Policies." Or, you can access the policies directly by going to <a href="http://www.marshall.edu/academic-affairs/?page_id=802">http://www.marshall.edu/academic-affairs/?page_id=802</a> Academic Dishonesty/ Excused Absence Policy for Undergraduates/ Computing Services Acceptable Use/ Inclement Weather/ Dead Week/ Students with Disabilities/ Academic Forgiveness/ Academic Probation and Suspension/ Academic Rights and Responsibilities of Students/ Affirmative Action/ Sexual Harassment  See the <a href="University Academic Calendar">University Academic Calendar</a> <a href="http://www.marshall.edu/calendar/academic/">(http://www.marshall.edu/calendar/academic/)</a> ) for course withdrawal dates.

# <u>Description as a Critical Thinking "CT" Course:</u>

Description as a	This course fulfills five of seven Cores I "CT" core domains. Primarily,
Critical Thinking "CT" Course:	it fulfills the core domain of <b>integrative thinking</b> through the use of mathematical and abstract thinking techniques of calculus to teach students how to construct and evaluate mathematical terms like limits, derivatives and integrals symbolically, how to approximate limits, derivatives and definite integrals from graphical data, and how to apply calculus techniques to find local and global extrema and further analyze the behavior of functions.
	Also, it fulfills the core domain of <b>creative thinking.</b> Students are able

to solve a given problem using various approach and different methods discussed in class. Also, it requires students to be able to write arguments on whether or not the properties in a definitions/argument hold true for given specific mathematical examples.

The course also fulfils the core domain of **communication fluency** by requiring students to be able to develop oral, written and/or visual communication skills in explaining the meaning of limits, derivatives and integrals, to be able to apply these definitions to specific problems and to write arguments on whether or not the properties in these definitions hold true for given specific mathematical examples.

Furthermore, this course fulfills the core domain of **inquiry based thinking** by teaching student how to formulate, derive or model a problem using certain hypothesis. Students will evaluate/study certain problem, analyze the problem with reasonable conclusion.

Lastly, this core fulfills the core domain of **quantitative thinking** by teaching students how to analyze real world problems in science, engineering and other field quantitatively, come up with a model that best describe the problem and investigate validity of the model.

# An understanding of fundamental concepts of calculus and an appreciation of its applications Developing critical thinking skills by applying calculus skills to real world problems Obtaining an understanding of the theory in science and engineering mathematics Being able use technology to help solve problems. Satisfying program requirements for mathematics,

### How each student learning outcome will be practiced and assessed in the course

science, and engineering majors

MTH 229 Student Learning Outcomes	How students will practice each outcome in MTH 229	How student achievement of each outcome will be assessed in MTH 229
Students will be able to identify and	Students will complete homework,	Students' understanding of
graph standard algebraic functions.	classwork, and quizzes to get practice	functions will be evaluated
(communication fluency)	and feedback.	through questions on 3 in-

Students will be able to communicate mathematics in writing and orally. (communication fluency)  Students will be proficient at finding limits, derivatives and integrals of functions. Students will understand the concept of functions and their applications. (integrative thinking)	Students will complete brief, low- stakes writing assignments as part of daily classwork and quizzes. Students will engage in peer review of written and oral explanations of concepts. Students will complete homework, classwork, and quizzes to get Practice and feedback.	class tests, 1 project and the comprehensive final exam.  Students will be assessed on written communication through questions on 3 inclass tests, 1 project and the comprehensive final exam.  Students will be assessed on solving equations through questions on 3 in-class tests, 1 project and the comprehensive final exam.
Students will be able to develop mathematical model to solve real world problem. (creative, inquiry based and quantitative thinking)  Students will be able to analyze real	Student will complete assigned mathematical projects.  Students will complete homework,	Students will be assessed on their modeling skills on 1 take home project.  Students will be assessed on
world problems in science, engineering and other field quantitatively.  (quantitative thinking)  Student will be able to interpret	classwork, and quizzes to get Practice on modeling questions.  Students will complete homework,	Model analysis, derivation and verification through questions on 1 project.  Students will be assessed on
symbolic and numerical results to answer real-world questions, and recognize when a result is invalid in the real world.  (quantitative thinking)	classwork, and quizzes to get Practice on modeling questions.	Model applications through questions on 1 project.
Students will be able to select a function to model a physical example and apply calculus techniques to make Predictions (inquiry based thinking)	Students will complete projects, homework and quizzes to get practice and feedback	Students' understanding of applied calculus will be evaluated through questions on 1 project.

# **Course Requirements / Due Dates**

Attendance: Attendance is required. *Unexcused absences for more than two weeks will result in a reduction of one letter grade for the semester; unexcused absences from twelve or more classes will result in an F*. You will not be allowed to take makeup quizzes or exams, homework, etc. unless you have a university excuse. If an excused absence results in missing quiz/exam/hw, then a make-up date (*within one week of absence*) must be scheduled with course instructor. **Coming late to class, and use of cell phone** will be counted as an unexcused absence. Consult your handbook regarding university excused absences.

<u>Homework</u>: Homework will be assigned weekly on Friday and collected on Monday before class. Late homework assignments are not accepted, except in extenuating circumstances or University-approved absences. Copies of Homework are listed on the last page.

<u>Quizzes</u>: There will be a brief quiz during class meetings on Monday and Friday. Make-up quizzes are only given in the event of a university-excused absence.

<u>Projects:</u> Projects will be given to students. Students are to work in group and present their work as a presentation during dead week. **For past project questions, visit my website at**<a href="http://science.marshall.edu/otunuga/">http://science.marshall.edu/otunuga/</a> and click **project.** 

<u>Tests</u>: There will be 3 in-class tests during the semester, 1 project and a comprehensive Final Exam. **For past exam questions, visit my website at** http://science.marshall.edu/otunuga/ and click old exam. If you know in advance that you will have an excused absence on a test date, please make arrangements to take the test early. Make-up exams will only be given in the event of a university-excused absence.

<u>Final Exam</u>: The final exam will be on **Monday December 7, 2015 from 5-7pm**. Make travel arrangements accordingly. Make-up/early tests will not be available to accommodate individual travel plans.

# **Grading Policy**

Attendance	25pts
Quizzes,	75pts
Homework assignments	50pts
Three major exams	300pts
Project	100pts
Final ( comprehensive ) exam	150pts
The grading scale is rigid.	
90.00 – 100	A
80.00 - 89.99	В
70.00 – 79.99	С
60.00 - 69.99	D
Below 60.00	F

# **Tentative Course Schedule**

Week	<u>Dates</u> Fall	Approximate schedule : Sections covered and topics	Actual Date
	2015		Covered
1		1.1 triangle inequality interval notation distance formula equation of circle ways to represent a function finding domain and range of a function vertical line test of whether y is a function of x on a graph increasing and decreasing functions even and odd functions sketching transformations of graphs: horizontal and vertical shifts, horizontal and vertical scaling  1.2 linear functions point-slope and slope intercept form for lines quadratic functions quadratic formula completing the square	
		1.3 polynomial functions rational functions and how to find their domains exponential functions and logarithmic functions with base a constructing new functions from algebra and composition	
2	8/31- 9/3	1.4 right triangle definitions of trig functions: SOH CAH TOA radians vs. degrees unit circle definitions of cosine and sine and the other trig functions graphs of trig functions basic trig identities  1.5 one to one functions horizontal line test solving for the inverse function for a 1 to 1 function sketching the graph of an inverse function by reflecting across the line y=x restricting the domain to define inverse for sine, cosine and tangent  1.6 logarithmic functions and algebraic properties of logarithms solving exponential and logarithmic equations	
Week	Dates Fall 2015	Approximate schedule : Sections covered and topics	Actual Date Covered
3	9/8- 9/11	<ul> <li>average vs. instantaneous velocity average rate of change as slope of a secant line instantaneous rate of change as a limit of average rate of change</li> <li>demonstrating the concept of a limit: using tables of values to estimate limits tables of values can give misleading answers about limits determining a limit by looking at the graph of a function notation for one-sided limits: from right side lim</li></ul>	
		$x \rightarrow a$ ways a limit can fail to exist:	

		the right hand and left hand limits don't agree the limit is $\infty$ $or$ $-\infty$	
		how infinite limits are related to <b>vertical asymptotes</b> ,	
		finding vertical asymptotes	
		2.3 properties of limits rules for limits of polynomial functions, rational functions, and trig functions	
4	9/14-	2.4 definition of <b>continuity</b> at a point: three conditions must be satisfied	
	9/17	using the definition of continuity and properties of limits to show continuity	
		at a given point identifying on a graph ways a function can have a discontinuity	
		one sided continuity	
		types of discontinuity points	
		finding discontinuity points of rational and piecewise functions classes of continuous functions	
		using laws of continuity to build continuous functions	
		using substitution method for finding limits of continuous functions	
		2.5 finding limits of piecewise functions where the pieces join limits of functions which agree with another function at all,	
		but possibly one point:	
		cancellation and rationalization techniques for $\frac{0}{0}$ <b>type limits</b>	
		2.6 using <b>Squeeze Theorem</b> and a geometrical argument to prove $\lim_{\theta \to 0} \frac{\sin \theta}{\theta} = 1$	
		important limits with trig functions	
5	9/21-9/24	2.7 definition of $\lim_{x \to \infty} f(x) = L$ and $\lim_{x \to -\infty} f(x) = L$	
		how horizontal asymptotes are related to limits at infinity limits at infinity for basic polynomial functions and rational functions	
		techniques for calculating limits at infinity	
		2.8 Intermediate Value Theorem and applications to locating zeros of functions	
		2.9 <b>formal</b> $\varepsilon$ $-\delta$ <b>definition</b> of limit	
		demonstrating a limit on a graph by finding the value of $\delta$ , given a specific value of $\varepsilon$	
		using the $arepsilon-\delta$ definition to <b>prove</b> that the limit of a function exists	
		formal $arepsilon-\delta$ definition of right hand and left hand limits	
		Exam 1	
6	9/28-	3.1 slope of tangent line is the limit of slope of secant line	
	10/1	using definition of derivative: $f'(a) = \lim_{h \to 0} \frac{f(a+h) - f(a)}{h}$ to	
		algebraically compute derivatives and to estimate	
		numerical value of derivatives when h is small	
		using derivative to find <b>slope</b> ( and <b>equation</b> ) of <b>tangent lines</b> 3.2 interpreting derivative as a function of x	
		$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$	
		Leibniz notation and operator notation for derivatives rules for derivatives:  constant rule, power rule, constant multiple rule, sum & difference rules	

			- 1
		formula for the derivative of natural exponential function $e^x$	
		differentiability implies continuity	
		how a function can fail to be differentiable	_
		3.3 <b>product rule</b> and <b>quotient rule</b> for derivatives	
7	10/5-	3.4 applications of derivatives: instantaneous rate of change,	
	10/8	instantaneous velocity, marginal cost	-
		3.5 notation for <b>2</b> <sup>nd</sup> and <b>higher order derivatives</b> higher derivatives of polynomials and exponential functions	
		acceleration and jerk	
		3.6 derivatives of sine and cosine	-
		derivatives of other trig functions	
8	10/12-	3.7 Chain Rule	
	10/15	power rule combined with chain rule	
		using chain rule with the other rules for derivatives	-
		3.8 finding derivatives by <b>Implicit Differentiation</b> using implicit differentiation to compute slope of tangent line at a given	
		point	
		using implicit differentiation to find derivatives of inverse functions,	
		e.g. inverse trig functions	_
		3.9 formula for the derivative of general exponential function $b^{\scriptscriptstyle x}$	
		change of base formula for logarithms	
		formula for the derivative of $\ln x$ and $\log_b x$	
		definitions of the 6 basic <b>hyperbolic functions</b> how hyperbolic identities compare to trig identities	
		derivatives of hyperbolic functions	
9	10/19-	3.11 applying chain rule to <b>related rates</b> word problems	-
	10/22	Exam 2	
		EXAMIL 2	
		4.1 <b>linearization</b> of a function: using the tangent line to approximate the	
		function	
		computing <b>differentials</b> and using them to approximate errors and	
- 10	10/00	relative error	
10	10/26- 10/29	4.2 recognizing absolute extrema vs. local extrema on a graph  Extreme Value Theorem for absolute extrema of any continuous function	
	10/29	on closed interval	
		Fermat's Theorem for local extrema	
		definition of a <b>critical point</b>	
		local extrema can only occur at critical numbers, but there are critical	
		numbers which don't have local extrema  3-step method of finding absolute max and min of a function on	
		a closed interval	
		Rolle's Theorem	
		4.3 proving the <b>Mean Value Theorem</b>	•
		using Mean Value Theorem to help prove a function has exactly	
		one real root using Mean Value Theorem to prove $f^{\prime}(x)=0$ on an interval implies	
		$f$ is constant there using ${f 1}^{ m st}$ derivative sign charts to determine increasing and decreasing behavior	
		1st Derivative (Sign Chart)Test for local extrema	
		4.4 using 2 <sup>nd</sup> derivative sign charts to determine concavity and points of inflection	•
		asing = derivative sign charts to determine concavity and points of ninection	

11	11/2-		
	11/4	4.5 using <b>L'Hopital's Rule</b> to find limits of $\frac{0}{0}$ and $\frac{\infty}{\infty}$ indeterminate forms	
	/	finding limits of products and differences indeterminate forms	
		4.6 using 1 <sup>st</sup> and 2 <sup>nd</sup> derivative sign charts to sketch graph of polynomial,	
		rational, and other types of functions	
		graphs which have horizontal, vertical and slant asymptotes	
		4.7 solving max-min word problems justifying that your answer is an absolute extremum: if there is	
		only one local extremum on an interval, then that	
		local extremum is absolute	
12	11/9-	4.8 Newton's Method for approximating zeros of a function	
12	11/12	examples where Newton's Method fails	
	11,12	4.9 definition of an <b>antiderivative</b>	
		finding the most general antiderivative	
		indefinite integrals and integral notation	
		basic rules for integration: integrals for polynomial and trig functions	
		using initial conditions to find particular solutions to	
		1 <sup>st</sup> order differential equations	
		Exam 3	
		5.1 <b>sigma notation</b> for summations	
		some basic formulas for summations, Bernoulli's formula	
		inscribed and circumscribed rectangles	
		left endpoint and right endpoint and midpoint approximations of area beneath curves	
13	11/16-	5.2 Riemann sums	
	11/19	computing definite integral by taking limit of Riemann sums	
		properties of definite integrals , including comparison theorem	
		5.3 using 1st <b>Fundamental Theorem of Calculus</b> to evaluate	
		definite integrals	
		5.4 using <b>2</b> <sup>nd</sup> <b>Fundamental Theorem of Calculus</b> to find derivative of definite integrals with respect to variables	
		in the limits of integration	
14	11/30-	5.5 <b>Net Change Theorem</b> : definite integral of a derivative gives the total change in the function evaluating	
	12/3	more definite integrals displacement as the integral of velocity	
		5.6 <b>method of u-substitution</b> for indefinite and definite integrals application to integrating even and odd functions	
		5.7 Defining natural logarithm as integrals indefinite integrals with formulas involving inverse trig functions	